

Quiz 7 Sections 4.1, 4.2, 4.3

Name: Solution

- ① Find the absolute maximum and the absolute minimum of the following function on the following closed, bounded interval:

$$f(x) = 10 + 6x - x^2 \quad \text{on } [-4, 4]$$

$$f'(x) = 6 - 2x$$

$$0 = 6 - 2x$$

$$6 = 2x$$

$3 = x$  is a critical number

$$f(-4) = 10 - 24 - 16 = -30 \quad ] \quad \begin{array}{l} \text{Minimum} \\ \text{Maximum} \end{array}$$

$$f(4) = 10 + 24 - 16 = 18$$

$$f(3) = 10 + 18 - 9 = 19 \quad ] \quad \text{maximum}$$

- ② Sketch the graph of a function with the following properties:

$$f'(x) > 0 \quad \text{when } x < 1$$

$$f'(x) < 0 \quad \text{when } x > 1$$

$$f''(x) > 0 \quad \text{when } x < 1$$

$$f''(x) < 0 \quad \text{when } x > 1$$

(Make up a function and draw it;

just make sure it satisfies the

statements on the left)

(There are many right answers)

